Two photon absorption, nonlinear refraction, and optical limiting in semiconductors

Eric W. Van Stryland
H. Vanherzeele
M. A. Woodall
M. J. Soileau
Arthur L. Smirl
Shekhar Guha
Thomas F. Boggess
North Texas State University
Center for Applied Quantum Electronics
Department of Physics
Denton, Texas 76203

Abstract. Two-photon absorption coefficients β₂ of ten direct gap semiconductors with band-gap energy $E_g$ varying between 1.4 and 3.7 eV were measured using 1.06 µm and 0.53 µm picosecond pulses. β₂ was found to scale as $E_g^{-3}$, as predicted by theory for the samples measured. Extension of the empirical relationship between β₂ and $E_g$ to InSb with $E_g = 0.2$ eV also provides agreement between previously measured values and the predicted β₂. In addition, the absolute values of β₂ are in excellent agreement (the average difference being <26%) with recent theory, which includes the effects of nonparabolic bands. The nonlinear refraction induced in these materials was monitored and found to agree well with the assumption that the self-refraction originates from the two-photon-generated free carriers. The observed self-defocusing yields an effective nonlinear index as much as two orders of magnitude larger than CS₂ for comparable irradiances. This self-defocusing, in conjunction with two-photon absorption, was used to construct a simple, effective optical limiter that has high transmission at low input irradiance and low transmission at high input irradiance. The device is the optical analog of a Zener diode.

Subject terms: nonlinear optics; two-photon effects; index of refraction; semiconductors.

Optical Engineering 24(4), 613-623 (July/August 1985).

CONTENTS

1. Introduction
2. Theory
3. Experiment and data
   3.1. Experiment
   3.2. Data
4. Comparison of β₂ values to theory
   4.1. Two-photon absorption theory
   4.2. Comparison to theory
5. Self-refraction
6. Optical limiter
7. Conclusion
8. Acknowledgments
9. References

1. INTRODUCTION

The ever-increasing role of semiconductors in light-wave technology has created a pressing demand for the characterization of the nonlinear optical properties of these materials. Semiconductors are attractive as elements in nonlinear optical devices because of their large and potentially extremely fast optical nonlinearities. A careful study of these macroscopic nonlinearities should allow one to determine the dependence of these nonlinearities on fundamental microscopic mechanical and electronic material properties (e.g., band gap, carrier lifetime, carrier effective mass, etc.). The data base formed by this information would then allow one not only to tabulate the materials that exhibit large nonlinearities but also to predict the specific material parameters that give rise to these high nonlinearities. This predictive capability is extremely important from the standpoint of searching for materials with large nonlinearities.

A study of the nonlinear optical properties of several semiconductors is presented here, and a relationship between the two-photon absorption (2PA) coefficient β₂ and other material properties is verified. Ten different materials were experimentally studied for which the incident photon energy $\hbar \omega$ is less than the direct band-gap energy $E_g$ but greater than $E_g/2$ so that two-photon absorption is allowed. Both 1.06 and 0.53 µm picosecond pulses were used in transmission experiments using semiconductors with $E_g$ ranging from 1.4 to 3.7 eV. We find that the 2PA coefficient β₂ is given by

$$\beta_2 = \frac{K \sqrt{E_p} f(2\hbar\omega/E_g)}{n^2 E_g^3},$$

where $K$ is a material-independent constant, $n$ is the linear refractive index, and $E_p$ is nearly material-independent for a wide variety of semiconductors. The function $f$, whose exact form depends on the assumed band structure, is a function only of the ratio of the photon energy $\hbar \omega$ to $E_g$, which determines the states that are optically coupled. The scaling given by Eq. (1) agrees with the most recent theories for two-photon absorption and allows for predictions of 2PA coefficients for other materials at other wavelengths given minimal material parameters. For example, extension of this scaling [see Eq. (21)] to InSb (300 K) at 10.6 µm predicts a β₂ of 6.8 cm/MW, which is in excellent agreement with recent experiments. Specifically, Miller et al. obtained a value of 8 cm/MW. Equation (1) is therefore

$*E_p = 2P/m \hbar^2$, where $P$ is the Kane parameter and $m$ is the electron mass (Ref. 2).
valid over a range of 20 in band-gap energy from the infrared to the visible. In addition, we find that the proportionality constant $K$ as calculated by Weiler for nonparabolic bands agrees with our experimentally determined $K$ to within better than 26%.

We used the experimentally determined 2PA coefficients along with a modified Drude theory (modified to include effects of interband transitions and band filling) to model the nonlinear refraction in these semiconductors. We quantitatively fit the predictions of this theory to beam propagation data obtained for CdSe and obtain excellent agreement when all of the nonlinear refraction is assumed to arise from the carrier generation. This is the contributions proportional to the photogenerated carrier density dominate the usual bound electron nonlinear refractive index changes. This has been previously shown to be the case for one-photon absorption in materials such as InSb at 5 $\mu$m and Si at 1 $\mu$m. We find that the effective nonlinear refraction can be two orders of magnitude larger than that for Cs$_2$ at comparable irradiances.

Finally, we utilized the combined effects of two-photon absorption and nonlinear refraction in GaAs to make an irradiance (fluence) limiting device. This device has high linear transmission at low irradiance (fluence) and low transmission at high irradiance (fluence). At very high irradiances, laser-induced melting is also involved in the limiting action. This device is passive, has picosecond turn-on time, and is the optical equivalent of a Zener diode.

In Sec. 2 we describe the model used and derive the equations needed to describe both the nonlinear transmission and the nonlinear refraction observed in the semiconductors studied. In Sec. 3 we outline the experimental procedure used to determine the two-photon absorption coefficients and present the experimentally determined 2PA coefficients. Section 4 presents a comparison of the 2PA data to theory for parabolic and nonparabolic bands with and without exciton corrections. In Sec. 5 we present the experiments and fits to the beam propagation data using the results of Sec. 2. We describe a semiconductor optical limiter based on 2PA and its design, operation, and uses in Sec. 6.

2. THEORY

The experimental configuration used throughout this work was one in which the sample was very thin compared to the confocal beam parameter, and moreover, any self-induced beam phase changes were small enough that beam propagation effects in the sample were negligible (i.e., self-action was "external," as described in Ref. 11). In this case the Maxwell wave equation for the propagation of the electric field $E$ can be written as

$$2\text{i}\kappa \frac{\partial E}{\partial z} = \text{i} \omega \sigma \mu_0 E - \frac{\omega^2}{2\epsilon_0} \chi^{(3)} |E|^2 E,$$  \hspace{1cm} (2)

where $\chi^{(3)}$ denotes the third-order nonlinear susceptibility and

$$\sigma = (\alpha + \sigma_{ex}\nu) \frac{\epsilon_0}{\mu_0} + \frac{\nu \epsilon_0 n^2}{m_{eh} \omega} \nu$$  \hspace{1cm} (3)

denotes the conductivity. Here, we have explicitly included the possibility of photogenerated carrier absorption through the term $\sigma_{ex}$, where $\sigma_{ex}$ is the total carrier cross section (holes plus electrons) and $N$ is the density of these carriers. Also, $\alpha$ is the usual residual linear absorption (e.g., band-tail absorption, impurity absorption, etc.), and $\mu_0$ is the reduced electron-hole effective mass. Writing the electric field as

$$E = A \text{e}^{\text{i} \Phi}$$  \hspace{1cm} (4)

with the irradiance given by $I = (n \epsilon_0 C/2) A^2$, Eq. (2) can be separated, giving

$$\frac{d\Phi}{dz} = -\alpha I - \beta_2 I^2 - \gamma_1 N$$  \hspace{1cm} (5)

and

$$\frac{d\Phi}{dz} = \beta_1 \nu - \gamma_1 N,$$  \hspace{1cm} (6)

where $\beta_2$, the two-photon absorption coefficient, is proportional to the imaginary part of $\chi^{(3)}$ and $\beta_1 = \omega \gamma/c$ is proportional to the real part of $\chi^{(3)}$. $\gamma$ is related to the more usual $n_2$ (esu) $= \nu \gamma/40 \pi$, where the right-hand side of the equation is in mks system units. $\gamma_1$ in Eq. (6) is given by

$$\gamma_1 = \frac{\mu_0^2 e^2 CP}{2n m_{eh} \omega}.$$  \hspace{1cm} (7)

The parameter $P$ is introduced here to account for contributions to the nonlinear refraction proportional to $N_{ex}$ but not explained by the Drude model. An example of such a contribution is that arising from interband transitions.

The equation governing the carrier generation is

$$\frac{dN}{dt} = \frac{\beta_1 I^2}{2 \kappa \omega},$$  \hspace{1cm} (8)

showing that for every two absorbed photons one electron-hole pair is generated. This equation is valid only for pulses short enough that recombination and diffusion can be neglected during the pulse. We assume this to be the case for our picosecond pulses.

We note that Eq. (5) for the irradiance is independent of the phase [Eq. (6)]. This is due to our assumption of a thin sample (i.e., no irradiance changes due to nonlinear refraction within the material). We can, therefore, solve Eq. (5) simultaneously with Eq. (8) for the beam attenuation in a sample of thickness $L$. These equations must be solved numerically unless the contribution to the absorption from the photogenerated carriers is negligible. We can estimate under what conditions this is true by finding the irradiance, denoted by $I_{cr}$, for which the carrier absorption is equal to the multiphoton absorption. An approximate relation is found in the limit of small total absorption as

$$I_{cr} = \frac{2 \sqrt{2 \pi} \omega}{\sigma_{ex} \nu (1 - R)}.$$  \hspace{1cm} (9)

where $R$ is the surface reflectivity and $t_b$ is the HW $1/e$ (half-width at $1/e$ of the maximum in irradiance) of the assumed Gaussian temporal profile pulses. This result was first given by Bechtel and Smith. Note that this critical irradiance is independent of $\beta_2$ since both the transmission change and the photogenerated carriers result from 2PA. Thus, materials with small $\beta_2$, which require high incident irradiance to observe a transmission change, will be the most likely materials to be affected by photogenerated carrier absorption.

The contribution to the change in transmission from these carriers is proportional to $t_b^{-1}$. Longer pulses of the same irradiance contain more energy and, therefore, produce more carriers. We can determine if these carriers are contributing to the nonlinear absorption by measuring the change in transmission for different pulse widths. We show in Sec. 3 that the irradiances used are well below $I_{cr}$ and that we can ignore photogenerated carrier absorption. This is the reason for using picosecond pulses, as discussed in Ref. 13. While we find the carrier absorption to be negligible, the refractive index change proportional to the carrier density [Eq. (6)] is definitely not negligible, as discussed in Sec. 5.

The solution to Eq. (5) with this assumption is

$$I(z,r,t) = \frac{(1 - R) \ell I(o, r, t) e^{-\alpha z}}{1 + q(z, r, t)},$$  \hspace{1cm} (10)

where $q(z, r, t) = \beta_1 I(o, r, t) (1 - R) (1 - e^{-\alpha z})/\alpha$. Inside the sample $j = 1$, and behind the sample $j = 2$ since there are two surface
reflections. Also, \( z \) is equal to \( L \), the length of the sample. The effect of the rear surface reflection on the absorption has been ignored but is not expected to lead to significant errors in the determination of \( \beta_2 \) for the samples used. Equation (11) can be rearranged to give the instantaneous transmission \( T' \) at each radial position of a sample of length \( L \) as
\[
T' = \frac{1 + q(L, r, t)}{1 - R}
\]
(11)

Since \( q(z, r, t) \) is directly proportional to \( I(o, r, t) \), a plot of \( T'^{-1} \) versus incident irradiance should yield a straight line whose intercept determines \( a \) and whose slope determines \( \beta_2 \). Experimentally, pulses of Gaussian spatial and temporal profiles are used, which requires spatial and temporal integration of Eq. (10). Taking into account the temporal and spatial integrals, we find for the pulse transmission
\[
T = \frac{2\alpha (1 - R)}{I_0 \sqrt{n \beta_2} e^{aL} - 1} \int_0^\infty \ln [1 + q(L, o, o) e^{-x^2}] \, dx
\]
(12)

where we have taken
\[
I(o, r, t) = I_o \exp \left[ -\left( \frac{r}{r_0}\right)^2 - \left( \frac{t}{t_0}\right)^2 \right]
\]
(13)

The resulting plot of \( T^{-1} \) versus \( I \) has a slight downward curvature caused by these integrations, since at the higher irradiances both the spatial and temporal profiles are broadened toward the rear of the sample (i.e., there is more 2PA at the middle, brightest part of the beam). Examples of plots of \( T^{-1} \) from Eq. (12) as a function of \( I_0 \) are shown in Figs. 5(a) and 5(b) of Sec. 3.

In order to model the beam profile of the pulse and its propagation, we now integrate Eq. (6) using Eq. (8) for \( N \) and Eq. (10) \((j = 1)\) for the irradiance to obtain an expression for the phase:
\[
\Phi(L, r, t) = \Phi(o, r, t) + \frac{\beta_1}{\beta_2} (1 - R) \ln [1 + q(L, r, t)] + \frac{(1 - R)^2 \gamma_1}{2\omega_0 \beta_2} \int_{-\infty}^{t} dt' F_1(t')
\]
(14)

where
\[
F_1(t) = a \ln [1 + q(L, r, t)] - \frac{q(L, r, t) a}{1 - e^{-aL}} \left[ 1 - \frac{e^{-aL}}{1 + q(L, r, t)} \right]
\]
(15)

Equations (10) \((j = 2)\) and (14) together completely describe the electric field at the exit plane of the sample. From these solutions for \( I(L, r, t) \) and \( \Phi(L, r, t) \), the field at any position outside the sample \( (L + z, r, t) \) can then be determined using the Huygens-Fresnel propagation formalism as
\[
E(L + z, r, t) = \frac{2\pi}{i\lambda z} \exp \left( \frac{i\pi^2}{\lambda z} \right)
\]
\[
\times \int_0^\infty \int_{-\infty}^{\infty} \exp \left( \frac{i\pi^2}{\lambda z} \right) J_0 \left( \frac{2\pi r'}{\lambda z} \right) d\tau' dt'
\]
(16)

What we measure in our experiments, using short pulses, is the fluence, given by
\[
F(L + z, r, t) = c e^{aL} \int_{-\infty}^{\infty} |E(L + z, r, t)|^2 \, dt
\]
(17)

Experimental results are compared with numerical evaluations of Eq. (17) and/or spatial integrals of Eq. (17), as described in Sec. 5.

3. EXPERIMENT AND DATA

3.1. Experiment

In the first set of experiments we measured the transmission of several semiconductors as a function of incident irradiance to determine their nonlinear absorption coefficients. The experimental arrangement is shown in Fig. 1. The laser source used was a microprocessor-controlled, passively mode-locked Nd:YAG laser that produced single amplified pulses of energy up to 7 mJ per pulse at 1.06 µm when operated in the TEMoo mode.* The pulse width could be varied between 40 and 150 ps (FWHM) by selecting etalons of varying thickness as the output coupler. The width of each pulse was monitored by measuring the ratio \( R \) of the square of the energy of the second harmonic (0.53 µm) pulse to the energy of the second harmonic (1.06 µm) pulse that was produced in a LiIO₃ crystal.‡ This ratio is directly proportional to the laser pulse width, provided that the spatial profile remains unchanged. This ratio was calibrated by measuring the pulse width using nearly background-free second-harmonic autocorrelation scans while accepting only pulses having a fixed ratio \( R \) within 15% of the preset value. To ensure that the ratio \( R \) was held fixed, and the autocorrelation data were as clean as those shown for 1.06 µm in Fig. 2.

Two different pulse widths of 40 and 150 ps were used in the transmission experiments on each sample at 1.06 µm. Since the output coupler etalons used to change the pulse width were optically contacted to a flat rotatable quartz plate, the beam line as well as the measured beam parameters remained fixed. (A few percent change in the beam spatial width probably caused by slight self-focusing in the beam was scaled properly. An example of such an autocorrelation scan is shown in Fig. 2 along with the best Gaussian fit. The autocorrelation width of 54 ps (FWHM) corresponds to a Gaussian pulse width of 38 ps (FWHM).

When 0.53 µm light was required, a temperature-tuned CDA (cesium dihydrogen arsenate) crystal was placed in the beam at the position indicated by the arrow in Fig. 1. Light at 1.06 µm was blocked by a polarizer and two 100% dielectric reflecting mirrors. Autocorrelation scans of the second-harmonic beam performed with an angle-tuned KD*P (potassium dihydrogen phosphate) crystal showed that these pulses scaled as the 1.06 µm pulse width divided by \( \sqrt{2} \) to within 10%, as expected for Gaussian-shaped pulses. Again the ratio \( R \) was held fixed, and the autocorrelation data were as clean as those shown for 1.06 µm in Fig. 2.

*Quantel model YG40, Quantel International, Inc., Santa Clara, Calif.
The relative error bars between one transmission experiment and the next, where only the pulse width was changed, were very small. While at high irradiances (a few GW/cm²) we did see a small pulse width dependence of the transmission in some samples, this difference was consistent with values for the free-carrier cross sections ($10^{-17}$ to $10^{-18}$ cm²). No pulse width dependence was observed at the low irradiance levels (0.5 GW/cm² at 1 µm) used to extract values of the 2PA coefficient. A calculation of $I_{cr}$ from Sec. 2 for typical samples at 1 µm gives $I_{cr} \sim 5$ GW/cm² for $\sigma_{ex} \sim 5 \times 10^{-18}$ cm². In fact, Eq. (9) considerably underestimates $I_{cr}$. From computer calculations, we find that $I_{cr}$ is several times larger, the difference arising mainly from the fact that the spatial irradiance averaging was ignored in the approximate expression. In addition, at 0.5 µm the contribution of photogenerated carrier absorption will be less than at 1 µm since $\hbar \omega$ increases and $\sigma_{ex}$ decreases, both leading to an increase in $I_{cr}$. The maximum experimental irradiance used to extract $\beta_2$ from the 0.53 µm data was, therefore, increased to 2 GW/cm². The above experimental considerations justify ignoring free-carrier absorption in calculating the transmitted irradiance [Eq. (5)].

The spatial beam profiles in both the horizontal and vertical directions were determined by scanning a 25 µm pinhole at the position of the sample. The beam size was adjusted at the sample by using pairs of collimating lenses. In all, four different spot sizes from 0.5 mm to 1.5 mm (FWHM) were used for the 1.06 µm data. At 0.53 µm the beam size used was 0.5 mm. In addition, the beam profiles were monitored on a vidicon to ensure that there were no hot spots, spurious reflections, or shot-to-shot beam width fluctuations. Figure 3 shows a representative pinhole scan for a 1.06 µm beam of FWHM 1.50 mm.

The incident energy was continuously varied using a stepping-motor-controlled rotating half-wave plate in combination with a fixed polarizer. This apparatus kept the polarization on the sample fixed and introduced no measurable beam walk with rotation angle. Previous experience indicates that other alternatives, e.g., rotating calcite polarizers, may cause the beam to walk across the sample and across the energy-monitoring detectors.

The choice of detectors, as well as the detection geometry, was also determined to be critical. As discussed in Sec. 5, the phase aberrations introduced on the beam by the two-photon-generated free carriers cause considerable defocusing so that the beam profile at the detector varies with incident irradiance. Figure 4 shows an example of this defocusing as observed in the near field behind a sample of CdTe. As the irradiance is increased the beam broadens and breaks up, as is characteristic for self-defocusing. Thus, any spatial non-uniformities in the detector response can lead to errors. Indeed, care must be exercised to ensure that "external" self-action does not result in overfilling the transmission detector—an occurrence that could result in an overestimate of $\beta_2$ (Ref. 19) or could result in optical limiting, as discussed in Sec. 6. We found, however, that by using large area detectors (1 cm²) with a measured spatial uniformity of better than 10% and placing them as close as possible to the sample (3 cm), these effects were eliminated. The detectors were also determined to be linear over their range of use and were absolutely calibrated with respect to a pyroelectric energy monitor that was in turn checked against two others. In addition, absorbing-type neutral density filters placed in front of these detectors were checked to have linear transmission over a range at least a factor of 10 greater than the range used in these experiments. Filters were never used to attenuate the beam prior to the sample. In addition, spike filters transmitting only 1.06 µm (0.53 µm) were placed directly in front of the detectors to reduce optical noise from the flash lamps.

*Gentec ED-100, Gentec Inc., Ste-Foy, Quebec, Canada
Table I lists the 10 samples used in these experiments. In all, eight different materials having either a zinc blende or wurtzite structure were investigated. All of the samples were II-VI materials except for GaAs, which is a III-V material. The thickest sample used (0.5 cm) was over 100 times thinner than the confocal beam parameter (the Rayleigh distance) used for this study. Experiments were performed on each single crystal sample for two orthogonal directions of linear polarization. Within our experimental accuracy, no anisotropy in the measured values for $\beta_2$ was observed. A 15% variation was reported in Ref. 26 for room temperature CdTe; however, the optical pulse width was not given. In addition, the absolute values of the 2PA coefficients reported there were an order of magnitude larger than those we measured. This may indicate the dominance of carrier absorption for long pulses. In ZnTe and the single-crystal CdTe, the light propagation direction $k$ was in the (110) direction, and in GaAs, $k$ was in the (111) direction. In CdSe, Cd$_{0.5}$Sn$_{0.5}$, and Cd$_{0.25}$Sn$_{0.75}$, $k$ was parallel to the c-axis, while in CdS and ZnO, $k$ was perpendicular to the c-axis. Examples of data used to extract the 2PA coefficient are shown in Figs. 5(a) and 5(b) for 1.06 $\mu$m and 0.53 $\mu$m, respectively. Each data point is the average of five laser firings. The solid line in Fig. 5(b) is a fit for CdSe using $\alpha = 0$ and $\beta_0 = 18$ cm/GW in Eq. (12). The solid line in Fig. 5(b) is a similar fit for ZnSe using $\alpha = 0.5$ cm$^{-1}$ and $\beta_0 = 5.5$ cm/GW at 0.53 $\mu$m. In all samples the linear absorption was small, and its value was unimportant in the determination of $\beta_2$. In both samples of ZnS the scattering was less than 10%.

Table I always had a larger $\beta_2$ than ZnS(clear). We conservatively estimate these relative error bars, which are important in determining the parametric dependence of $\beta_2$ as discussed in the next section, to be $\pm 25\%$.

In the second set of experiments (to be discussed in Sec. 5) we replaced the transmission detector in Fig. 1 by either a vidicon tube interfaced with an optical multichannel analyzer or a 25 $\mu$m pinhole placed at various radial positions and longitudinal distances from the sample. We then monitored the spatial beam profile of the transmitted beam using the vidicon, or we monitored the pinhole transmission as a function of incident irradiance. In Sec. 5 we describe the use of Eq. (17) to theoretically fit both of these results.

4. COMPARISON OF $\beta_2$ VALUES TO THEORY

4.1. Two-photon absorption theory

We make three separate comparisons in this section. We first compare our experimentally determined $\beta_2$ values with the theory of Refs. 3–5 using a parabolic band structure. Excellent agreement is found for all materials except ZnTe. We then use the nonparabolic theory and again find good agreement for all materials except ZnTe. As shown by Weiler, the differences between the parabolic and nonparabolic theories are minor so that this fit is expected. We then include exciton correction factors, as given by Lee and Fan and as calculated by Weiler and we find that when these are included, ZnTe nearly fits the dependencies shown by the other materials.

As stated in Ref. 5, the parametric dependence of $\beta_2$ on $E_\text{p}$ and $E_\text{g}$ was first explicitly pointed out by Pidgeon et al., although it was present in the calculations of Basov et al. The band structure and transition scheme used by Pidgeon et al. is shown in Fig. 6. Calculations using this scheme have been performed for parabolic and nonparabolic bands. They found

$$\beta_2 = \frac{4\pi e^4}{\sqrt{2}\omega_0} \frac{\sqrt{E_\text{p}}}{n^2 E_\text{g}^2} \left(\frac{2\omega_0}{E_\text{g}}\right) = 53.8 \frac{\sqrt{E_\text{p}}}{n^2 E_\text{g}^2} \left(\frac{2\omega_0}{E_\text{g}}\right) \quad (18)$$

**TABLE I. Material Parameters and Two-Photon Absorption Coefficients of the Materials Studied**

<table>
<thead>
<tr>
<th>Material</th>
<th>Form</th>
<th>$n(\lambda)$</th>
<th>$E_g(\text{eV})$</th>
<th>$E_p(\text{eV})$</th>
<th>$E_p/E_g$</th>
<th>$\beta_\text{2exp}(\text{cm}/\text{GW})$</th>
<th>$\beta_\text{2theor}(\text{cm}/\text{GW})$</th>
</tr>
</thead>
<tbody>
<tr>
<td>ZnTe($^c$)</td>
<td>Z</td>
<td>2.79($^c$)</td>
<td>2.26($^i$)</td>
<td>19.1</td>
<td>0.004($^c$)</td>
<td>4.5</td>
<td>0.89</td>
</tr>
<tr>
<td>CdS$<em>{0.25}$Se$</em>{0.75}$($^c$)</td>
<td>Z</td>
<td>2.40($^c$)</td>
<td>2.67($^c$)</td>
<td>24.2</td>
<td>0.009($^c$)</td>
<td>5.5</td>
<td>4.27</td>
</tr>
<tr>
<td>Cd$<em>{0.3}$Se$</em>{0.7}$($^c$)</td>
<td>Z</td>
<td>2.60($^c$)</td>
<td>2.46($^c$)</td>
<td>21</td>
<td>0.012($^c$)</td>
<td>5.5</td>
<td>4.87</td>
</tr>
<tr>
<td>ZnS($^i$)</td>
<td>Zp(clear)</td>
<td>2.40($^i$)</td>
<td>3.66($^i$)</td>
<td>20.4</td>
<td>0.010($^i$)</td>
<td>2.0</td>
<td>2.10</td>
</tr>
<tr>
<td>ZnS($^f$)</td>
<td>Zp(yellow)</td>
<td>2.40($^f$)</td>
<td>3.68($^f$)</td>
<td>20.4</td>
<td>0.010($^f$)</td>
<td>3.5</td>
<td>2.10</td>
</tr>
<tr>
<td>ZnSe($^d$)</td>
<td>Zp</td>
<td>2.70($^d$)</td>
<td>2.67($^d$)</td>
<td>24.2</td>
<td>0.008($^d$)</td>
<td>5.5</td>
<td>4.27</td>
</tr>
<tr>
<td>CdS($^c$)</td>
<td>W</td>
<td>2.60($^c$)</td>
<td>2.46($^c$)</td>
<td>21</td>
<td>0.012($^c$)</td>
<td>5.5</td>
<td>4.87</td>
</tr>
<tr>
<td>ZnS($^h$)</td>
<td>W</td>
<td>2.05($^h$)</td>
<td>3.20($^h$)</td>
<td>21</td>
<td>0.020($^h$)</td>
<td>5.0</td>
<td>4.77</td>
</tr>
</tbody>
</table>

(a) Z = zinc blende; W = wurtzite; $p$ = polycrystalline
(b) Values taken from Ref. 20. For values not listed in this Reference, the value of 21 eV was assumed.
(c) Cleveland Crystals, Euclid, Ohio
(d) II-VI, Inc., Saxonburg, Pa.
(e) Morgan Semiconductors, Garland, Tex.
(f) CVD Inc., Woburn, Mass.
(g) Raytheon Co., Bedford, Mass.

(b) Atomergic Chemicals, Plainview, N.Y.
(i) Ref. 21
(j) Ref. 22
(k) Ref. 23
(l) These values obtained by linear extrapolation as a function of composition between the known values for CdS and CdSe. See Ref. 24.
(n) Ref. 25
(o) Ref. 4

## 3.2. Data

The results of these measurements of the 2PA coefficients are shown in Figs. 5(a) and 5(b) for 1.06 $\mu$m and 0.53 $\mu$m, respectively. Each data point is the average of five laser firings. The solid line in Fig. 5(b) is a fit for CdSe using $\alpha = 0$ and $\beta_0 = 18$ cm/GW in Eq. (12). The solid line in Fig. 5(b) is a similar fit for ZnSe using $\alpha = 0.5$ cm$^{-1}$ and $\beta_0 = 5.5$ cm/GW at 0.53 $\mu$m. In all samples the linear absorption was small, and its value was unimportant in the determination of $\beta_2$. In both samples of ZnS the scattering was significant, and this loss mechanism was included in the model as linear absorption. In the latter case, the effect of the choice of $\alpha$ on $\beta_2$ was less than 10%.

The results of these measurements of the 2PA coefficients are given in the next to the last column of Table I. The absolute error bars on the values of $\beta_2$ are estimated to be $\pm 40\%$. The relative error bars of $\beta_2$ determined from one sample to the next are considerably better, as observed by measuring all the samples in sequence for each spot size and each pulse width. For example, ZnS(yellow) listed in
Fig. 5. Inverse transmission versus incident irradiance for (a) CdSe at 1.06 \( \mu m \) and (b) ZnSe at 0.53 \( \mu m \). The solid lines are fits using Eq. (12).

where \( E_p \) and \( E_g \) are in eV and \( \beta_2 \) in cm/GW in the last expression. Here, \( m \) is the electron mass, \( e \) is the electron charge, \( c \) is the speed of light in vacuum, and \( n \) is the refractive index. The values of \( E_g \), \( E_p \), and \( n \) for each material are listed in Table I. It is important to note that for both parabolic and nonparabolic bands, the parametric dependencies on \( n \), \( E_g \), and \( E_p \) predicted by the theories are the same. In addition, as pointed out in Ref. 5 these dependencies are independent of crystal structure. The differences lie in the function \( f \) and the ratio of \( f \) to \( E_g \) (i.e., which states are optically coupled). Weiler 4 corrected an error in the calculation of \( f \) in Ref. 3 and obtained the following expression using parabolic bands:

\[
\begin{align*}
  f(x) &= \frac{2^5}{\sqrt{6}} \left( 4 + \frac{29 \sqrt{2}}{12} \right) \left[ \frac{(x - 1)^{3/2}}{x^5} \right] = 96.9 \left[ F_2(x) \right], \tag{19}
\end{align*}
\]

where \( F_2(x) \) is the same function defined in Ref. 5. For nonparabolic bands, Weiler 4 found for \( \Delta \ll E_g \)

\[
\begin{align*}
  f_{np}(x), \Delta \ll E_g &= \frac{32 \sqrt{3}}{5} \left( \frac{x - 1}{x^3} \right)^{3/2} \times \left[ \frac{3 \sqrt{x}}{\left( \frac{3}{2} x - 1 \right)^{3/2}} + \frac{(x + 1)^{3/2}}{3x^5} (x^4 + 2x^2 + 6) \right]. \tag{20}
\end{align*}
\]

As shown in Ref. 4, the differences between \( f_{np} \) for \( \Delta \ll E_g \) and \( \Delta \gg E_g \), where \( \Delta \) is the split-off energy shown in Fig. 6, are small. The expression for \( \Delta \gg E_g \) is

\[
\begin{align*}
  f_{np}(x), \Delta \gg E_g &= 16 \sqrt{\frac{2}{3}} \frac{(x - 1)^{3/2}}{x^3} \times \left[ \frac{\sqrt{x}}{\left( \frac{3}{2} x - 1 \right)^{3/2}} + \frac{6}{45} \frac{(x + 1)^{3/2}}{x^5} \left( \frac{9}{16} x^4 + \frac{5}{2} x^2 + 6 \right) \right]. \tag{21}
\end{align*}
\]

Exciton corrections to values of \( \beta_2 \) have been predicted by Lee and Fan. 27 Weiler 4 has evaluated these corrections in terms of the ratio \( \epsilon \) of the exciton binding energy \( E_b \) to the band-gap energy \( E_g \). These ratios are listed in Table I. We reproduce in Fig. 7 (from Ref. 4) the results of these calculations of the excitonic enhancement \( g_{ex} \) of \( \beta_2 \) as a function of \( f \) to \( E_g \) for various values of \( \epsilon \).

4.2. Comparison to theory

Figure 8 shows a log-log plot of \( \beta_2 \) scaled by \( n^2/(\sqrt{E_p F_2}) \) [see Eq. (19) for \( F_2 \)] as a function of \( E_g \). The solid line is a least squares fit to the data (excluding ZnTe) for a line having a slope of -3 to account for the \( E_g^3 \) dependence of \( \beta_2 \). Clearly, the parametric dependences using this parabolic theory fit the data very well except for ZnTe. This single parameter fit yields a 2PA coefficient given by the following equation:

\[
\begin{align*}
  \beta_2 &= (3.1 \pm 0.5) \times 10^3 \frac{\sqrt{E_p F_2} \left( \frac{2\epsilon \omega}{E_g} \right)}{n^2 E_g^3}, \tag{22}
\end{align*}
\]

where again \( E_p \) and \( E_g \) are in eV and \( \beta_2 \) is in cm/GW. The values predicted from Eq. (22) are listed in the last column of Table I for each material. The value of the constant [\( 3.1 \times 10^3 \) in Eq. (22)] predicted by theory from Eqs. (18) and (19) is 5.21 \( \times 10^3 \), so that the absolute values of the experimentally determined \( \beta_2 \) values are, on
The values of the exciton binding energy $E_b$ to the band-gap energy $E_g$ (reproduced with permission from Ref. 4).

This correction factor has been calculated only for parabolic bands.27

Closer to $A < E_g$, and may be partially responsible for scatter in the case for these materials lies in between the two theories, although almost identical fit, except in this case the difference between theory and experiment observed for ZnTe ($g_{ex} = 4.3$)² has been removed by including excitonic enhancement. However, the overall fit to the parametric dependence (again the straight line is a least squares fit) is somewhat worse. This may be attributed to our lack of accuracy in calculating $g_{ex}$. Note that for most materials, $g_{ex}$ is of the order of 2, even when the coupled states are well above the gap (see Fig. 7). Consequently, when excitonic enhancement is included for parabolic bands, the absolute $\beta_2$ values predicted by theory are a factor of 3.3 larger than those measured.

The reason that the exciton enhancement for ZnTe is considerably larger than for the other materials is that at 1.06 $\mu$m, two photons couple states only 3.5% above the gap, where excitonic effects should be greatest, as shown in Fig. 7. We should point out, however, that we have only one material for which the coupling is this close to the gap, and the error bars for this material are larger than for the other materials. ZnTe damaged easily, allowing us to use a small spot size only and limiting the range of irradiances for fitting $\beta_2$. On the other hand (as shown in Fig. 8), where there is overlap between the data taken here and the data taken by Bechtel and Smith,¹³ the agreement is excellent. They also obtained a large $\beta_2$ for ZnTe.

Two other data points listed in Table I and shown in Figs. 8, 9, and 10 require comment. The polycrystalline CdTe sample gave an experimental $\beta_2$ lower than the single-crystal CdTe sample. It is
designed as a 10.6 μm optical window and is doped with $10^{17}$ cm$^{-3}$ of indium. It is not understood at present if or how these impurities lower the measured $\beta_2$. The ZnS(yellow) sample is a chemical vapor deposition grown sample that has a yellow appearance caused by crystal lattice imperfections that can be annealed out by a special heat treatment process. The ZnS(clear) is the same starting material that has undergone this heat treatment. It appears water clear, and its linear transmission cutoff is shifted into the UV. The indication from the data presented here is that not only has the linear absorption in the visible and near-UV been reduced, but the two-photon absorption at 0.5 μm has also been reduced by this heat treatment. That is, defects may be contributing to $\beta_2$. This may also be true for the ZnTe sample at 1 μm since it damaged easily.

5. SELF-REFRACTION

In this section we present results for the beam propagation behind the sample, given the irradiance and phase distribution of Eqs. (10) and (14). Equation (17) describes the fluence at any point $z$ behind the sample. We present data here using a beam of width 1.70 mm (FWHM) incident on the CdSe sample listed in Table I, which is placed near the beam waist. Thus, $\Phi(0,0,t)$ is taken to be zero in Eq. (14). The transmitted signal was monitored at distances of 0.5 m and 2 m behind the sample, both of which are near-field regions. Figure 11 illustrates the change in the beam profile with irradiance at $z = 0.5$ m (using 92 ps FWHM pulses) as displayed on the vidicon. This scan is a narrow slice through the center of the beam that is equivalent to a pinhole. The dashed line is a fit to Eq. (17) as a function of distance from the sample. We present here a beam of 1.70 mm (FWHM) with a constant irradiance (fluence) of a pulse incident upon sensitive optical components or as a regulator to smooth optical transients. This device is the optical analog of a Zener diode.

Optical limiting by nonlinear absorption in semiconductors was proposed and demonstrated in the late 1960s. Moreover, nonlinear refraction combined with spatial filtering has been used to demonstrate optical limiting in liquid and gas-filled cells. Here we demonstrate optical limiting in GaAs. Below the melting threshold, what we have done differently is to use not only nonlinear absorption but also nonlinear refraction together with spatial filtering to construct a more effective device. Above the melting threshold, we also take advantage of a solid-to-liquid phase transition, which affects the reflectivity and transmission.

The geometry we used for optical limiting is shown in Fig. 15. A single 40 ps (FWHM) 1.06 μm pulse was focused to a 100 μm (FWHM) spot at the surface of the GaAs with a 465 mm focal length lens $L_1$. The transmitted beam was collected and collimated by a 381 mm focal length lens $L_2$ placed one focal length behind the sample. The recollimated beam then passed through a 2 mm diameter aperture placed one focal length beyond $L_2$ and directly in front of a photodetector. The sample used was nearly identical to the sample listed in Table I. The limiting capabilities of the device are shown by the triangles in Fig. 16. At low input energies (<0.5 μJ), the device response was linear and was consistent with the 45% linear transmission of the GaAs and the 73% transmission of the pinhole. Above 10 μJ input, the output energy was essentially clamped at 1 μJ. The device continued to limit for input energies greater than 1 mJ. Over the full range of operation, the system transmission was reduced from 33% to 1%. Notice that regulation continued for input energies far above the GaAs single-shot melting threshold of 0.9 J/cm$^2$ (indicated by the arrow in Fig. 16). Above the melting threshold, the GaAs was translated before each firing so that each pulse irradiated virgin material.

Below the irradiance required for melting, as the input energy was increased, the transmission of the GaAs was reduced by 2PA. In this
regime, the amplitude of the spatial beam profile transmitted by the GaAs was distorted solely by 2PA, and the phase was distorted by index changes associated with the 2PA-generated free carriers, as discussed in Secs. 2 and 4. The self-diffraction associated with this regime, the amplitude of the spatial beam profile transmitted by the GaAs was distorted solely by 2PA, and the phase was distorted by index changes associated with the 2PA-generated free carriers, as discussed in Secs. 2 and 4. The self-diffraction associated with this

above the melting threshold, the increase in the reflectivity and absorptivity of the molten region further reduced the GaAs transmission and further distorted the amplitude profile of the transmitted beam.

The contribution of 2PA and nonlinear reflection to the limiting action can be separated from the contribution of nonlinear refraction by carefully collecting all of the transmitted energy with the pinhole removed, as shown in Fig. 16. These results are shown by the circles in Fig. 16. Below \( E_{TH} \), the nonlinear transmission is dominated by 2PA and can be fit by a 2PA coefficient of 26 cm/GW.10 The value of

---

Fig. 12. Transmitted on-axis fluence as a function of incident irradiance at a distance of 0.5 m behind the sample: (a) 92 ps FWHM pulses and (b) 43 ps FWHM pulses. The solid lines are numerically calculated from Eq. (17).

Fig. 13. Transmitted on-axis fluence as a function of incident irradiance at a distance of 2.0 m behind the sample: (a) 92 ps FWHM pulses and (b) 43 ps FWHM pulses. The solid lines are numerically calculated from Eq. (17).

Fig. 14. Transmitted fluence measured at a point 1.1 mm off-axis as a function of incident irradiance at a distance of 0.5 m behind the sample: (a) 92 ps FWHM pulses and (b) 43 ps FWHM pulses. The solid lines are numerically calculated from Eq. (17).

Fig. 15. Schematic of GaAs optical limiter.

Fig. 16. Device response with (triangles) and without (circles) the 2 mm aperture in place. \( E_{TH} \) represents the single-shot melting threshold.
26 cm/GW reported in Ref. 10 for the 2PA coefficient $\beta_2$ of GaAs is nearly identical to the value of 23 cm/GW shown in Table 1 and indicates the confidence in the values of $\beta_2$. These measurements of $\beta_2$ on GaAs were made independently with a nearly identical laser system. Above $E_{TH}$, the problem becomes much more complicated and is outside the scope of this paper. In this regime, the central region of the pulse that arrives after melting is initiated is heavily attenuated and reflected by the molten layer of GaAs. In addition, there is considerable evaporation of material for fluences more than $\sim 10\%$ above the melting threshold. It is clear, however, that the transition from below to above threshold is a smooth one. That is, there is no discontinuity in limiter response at threshold.

It is interesting to compare the contributions of 2PA and self-diffraction just below the melting threshold. At an input energy of 80 $\mu$J, 2PA acting alone has reduced the transmission by a factor of five. On the other hand, the combined effects of 2PA and self-diffraction have reduced the transmission by a factor of 30. Thus, the present configuration is a considerable improvement over limiters that utilize 2PA exclusively.

We should also contrast the present switch with the Si device demonstrated in Ref. 36 that utilizes indirect absorption, free-carrier absorption, self-diffraction, and solid-liquid phase change to limit energetic pulses at 1 $\mu$m. The nonlinear absorption in Si at 1 $\mu$m is strictly fluence-dependent, and the device operation is independent of pulse width for pulse widths shorter than the carrier recombination time. The present device is considerably more complicated. The nonlinear absorption, which is dominated by 2PA, is irradiance-dependent, while the nonlinear refractive index that arises from the 2PA-generated free carriers is a time-integrated effect that persists for the duration of the carrier lifetime. Nevertheless, the carrier cannot be generated without a sufficiently intense pulse, which in practice restricts this device to operation with short pulses. However, the limiting pulse energy can be varied considerably by changing the geometry (e.g., using a very short focal length lens $L_j$ in Fig. 15 will lower the limiting energy). An advantage of the present device (and 2PA-based optical limiters in general) is that other contributions to $\beta_2$ (e.g., other bands) cause small effects.

7. CONCLUSION

The material parameter dependence found for a wide variety of semiconductors, as discussed in Sec. 3, allows us to predict, with reasonable confidence, the two-photon absorption coefficient of other materials at other wavelengths. This includes, for example, mixed ternary compounds. Thus, the 2PA at a particular wavelength can be tailored for a specific application.

The fact that this scaling fits the data so well implies that all of the important material parameters have been included in the theory and that other contributions to $\beta_2$ (e.g., higher bands) cause small effects. One possible deviation from the predicted scaling is the effect of excitons. We have one material (ZnTe) that indicates that such effects may be important. If we attempt to extend this theory into the UV, we find that the predictions are in general considerably lower than in the experiments; however, a general trend can be found. If the coupled states are well above the gap, the deviations are relatively small, on the order of a factor of four or five. As the coupled states get close to the gap, however, the deviation increases rapidly. For example, in Rbl at 266 nm where $\Delta \omega_c/E_p = 1.47$, the experimentally measured 2PA coefficient of 2.49 cm/GW is 3.7 times larger than predicted by Eq. (22). At a wavelength of 355 nm where $\Delta \omega_c/E_p = 1.10$, however, the measured 2PA coefficient of 0.08 cm/GW is 14 times larger than predicted. This trend is maintained for the limited data available. Considering color centers as excitons with large binding energies, such large correction factors may be accounted for.

The role of excitons and color centers in 2PA needs further study. A study of the wavelength dependence of 2PA near the gap using a continuously tunable laser should help clarify the role of excitons.

It is interesting to look at the history of the measurement of 2PA coefficients. Figure 17 shows experimental values of $\beta_2$ reported for GaAs and CdSe for years beginning with 1966. This figure illustrates the fairly steady decrease in reported values as both the lasers and the experimental techniques were refined. Much of the earlier data were obtained with nanosecond pulsed lasers where photogenerated carrier absorption is expected to dominate. Additionally, in some instances multimode lasers were used. An additional experimental problem not previously recognized that can lead to an overestimate of $\beta_2$ is that the extreme defocusing present may allow some of the transmitted light to go undetected.

While this defocusing may be an experimental difficulty in determining $\beta_2$, it can be extremely useful for nonlinear optical devices such as the limiter discussed in Sec. 6. We found that this defocusing was quantitatively explained by attributing all of the nonlinear refraction to the buildup of excited carriers, although the simple Drude theory had to be modified to allow for interband transitions. These fits indicate that interband transitions may actually dominate the refractive index change in these two-photon absorbers. In addition, we demonstrated a simple but effective optical limiter based on two-photon absorption, the associated self-defocusing, and spatial filtering. By choosing a substance with the proper material parameters and a specific geometry, this limiting can be tailored to suit a specific need. Clearly, further applications of the combined action of 2PA and self-refraction in nonlinear optical devices have been and will be found.

8. ACKNOWLEDGMENTS

The authors are most grateful to B. S. Wherrett for many stimulating and lengthy discussions. This research was supported with funds from the National Science Foundation (ECS #8310625), the Office of Naval Research, the Defense Advanced Research Projects Agency, and The Robert A. Welch Foundation.

9. REFERENCES

TWO PHOTON ABSORPTION, NONLINEAR REFRACTION, AND OPTICAL LIMITING IN SEMICONDUCTORS